

## Algoritmo para construção de um código de Huffman otimizado

**Input:** a sequence of  $n$  frequencies ( $N \geq 2$ ).

**Output:** a rooted tree that defines an optimal Huffman code.

**procedure** *huffman(f,n)*

**if**  $n = 2$  **then**

**begin**

            let  $f_1$  and  $f_2$  denote the frequencies;

            let  $T$  be as in figure 7.1.9;

**end**

**else**

        let  $f_i$  and  $f_j$  denote the smallest frequencies;

        replace  $f_i$  and  $f_j$  in the list by  $f_i + f_j$ ;

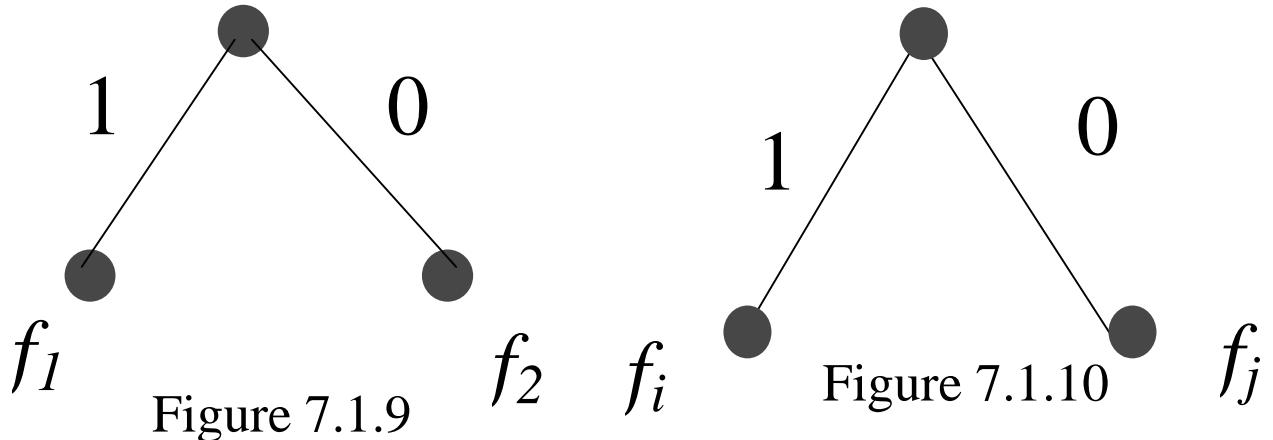
$T' := huffman(f, n-1)$ ;

        replace vertex in  $T'$  labeled  $f_i + f_j$  by the tree shown in figure 7.1.10 to obtain tree  $T$ ;

**end;**

**return**  $T$ ;

**end** *huffman*;



## Procurando uma “spanning tree” : busca em largura

**Input :** a connected graph  $G$  with vertices ordered  $V = \{v_1, v_2, \dots, v_n\}$

**Output :** a spanning tree  $T$ .

**procedure**  $bfs(V, E)$

//  $V'$  := vertices of spanning tree  $T$ ;  $E'$  := edges of spanning tree  $T$ ;

//  $v_1$  is the root of the spanning tree ;  $S$  is an ordered list ;

$S := (v_1);$

$V' = \{v_1\};$

$E' = \emptyset;$

**while**  $true$  **do**

**begin**

**for** each  $x \in S$ , in order, **do**

**for** each  $y \in V - V'$ , in order, **do**

**if**  $(x, y)$  is an edge **then**

                add edge  $(x, y)$  to  $E'$  and  $y$  to  $V'$ ;

**if** no edges were added **then**

**return**  $T$ ;

$S :=$  children of  $S$  ordered consistently, with the original vertex ordering;

**end;**

**end**  $bfs$ .

## Procurando uma “spanning tree” : busca em profundidade

**Input :** a connected graph  $G$  with vertices ordered  $V = \{v_1, v_2, \dots, v_n\}$   
**Output :** a spanning tree  $T$ .

**procedure**  $dfs(V, E)$   
//  $V'$  := vertices of spanning tree  $T$ ;  $E'$  := edges of spanning tree  $T$ ;  
//  $v_1$  is the root of the spanning tree ;  
 $V' := \{v_1\}$ ;  $E' := \emptyset$  ;  $w := v_1$ ;  
**while**  $true$  **do**  
**begin**  
    **while** there is an edge  $(w, v)$  that when added to  $T$  does not create a cycle  
        in  $T$  **do**  
        **begin**  
            choose the edge  $(w, v_k)$  with minimum  $k$  that when added to  $T$  does  
            not create a cycle in  $T$  ;  
            add  $(w, v_k)$  to  $E'$  ; add  $v_k$  to  $V'$ ;  
             $w := v_k$  ;  
        **end**;  
    **if**  $w = v_1$  **then**  
        **return**  $T$  ;  
     $w :=$  parent of  $w$  in  $T$  ; // Backtrack.  
**end**;  
**end**  $dfs$ .

## Algoritmo de Prim

```
procedure prim( $w, n, s$ )
//  $v(i) = 1$  if vertex  $i$  has been added to minimal spanning tree (mst).  $v(i) = 0$  otherwise.
for  $i := 1$  to  $n$  do
     $v(i) := 0$  ;
     $v(s) := 1$  ; // add start vertex to mst.
     $E := \emptyset$  ; // begin with an empty edge set.
for  $i := 1$  to  $n - 1$  do // put  $n - 1$  edges in the minimal spanning tree.
begin
     $min := \infty$  ; // add edge of minimum weight with one vertex in mst and one vertex not in mst.
    for  $j := 1$  to  $n$  do
        if  $v(j) = 1$  then //  $j$  is a vertex in mst.
        for  $k = 1$  to  $n$  do
            if  $v(k) = 0$  and  $w(j,k) < min$  then
            begin
                 $add\_vertex := k$  ;  $e := (j,k)$  ;  $min := w(j,k)$  ;
            end;
         $v(add\_vertex) := 1$  ; // put vertex and edge in mst.
         $E := E \cup \{e\}$  ;
    end ;
return  $E$  ;
end prim.
```

## Algoritmo para construção de uma árvore de busca binária

**Entrada:** uma sequência  $w_1, \dots, w_n$ , de palavras distintas e o comprimento

$n$  da sequência.

**Saída:** uma árvore de busca binária  $T$ .

**procedure** *make\_bin\_search\_tree*(*w*, *n*)

let  $T$  be the tree with one vertex, *root* ;

store  $w_1$  in *root* ;

**for** *i* := 2 **to** *n* **do**

**begin**

*v* := *root* ;

*search* := *true* ; // find spot for  $w_i$

**while** *search* **do**

**begin**

*s* := word in *v* ;

**if**  $w_i < s$  **then**

**if** *v* has no left child **then**

**begin**

add a left child *l* to *v* ;

store  $w_i$  in *l* ;

*search* := *false* ; // end search

**end**

**else**

*v* := left child of *v* ;

**else**

**if** *v* has no right child **then**

**begin**

add a right child *r* to *v* ;

store  $w_i$  in *r* ;

*search* := *false* ; // end search

**end**

**else**

*v* := right child of *v* ;

**end;**

**return** *T* ;

**end** *make\_bin\_search\_tree*.

## Percorso “preorder”

**Input :**  $PT$ , the root of a binary tree

**Output :** dependent on how process command is interpreted.

If process is equivalent to print, then the output  
is the vertex visiting sequence.

**procedure** *preorder*( $PT$ )

**if**  $PT$  is empty **then**

**return** ;

process  $PT$  ;

$l :=$  left child of  $PT$  ;

*preorder*( $l$ ) ;

$r :=$  right child of  $PT$  ;

*preorder*( $r$ ) ;

**end** *preorder*.

## Percorso “inorder”

**Input :**  $PT$ , the root of a binary tree

**Output :** dependent on how process command is interpreted.

If process is equivalent to print, then the output  
is the vertex visiting sequence.

**procedure** *inorder*( $PT$ )

**if**  $PT$  is empty **then**

**return** ;

$l :=$  left child of  $PT$  ;

*inorder*( $l$ ) ;

process  $PT$  ;

$r :=$  right child of  $PT$  ;

*inorder*( $r$ ) ;

**end** *inorder*.

## Percorso “postorder”

**Input :**  $PT$ , the root of a binary tree

**Output :** dependent on how process command is interpreted.

If process is equivalent to print, then the output  
is the vertex visiting sequence.

**procedure** *postorder*( $PT$ )

**if**  $PT$  is empty **then**

**return** ;

$l :=$  left child of  $PT$  ;

*postorder*( $l$ ) ;

$r :=$  right child of  $PT$  ;

*postorder*( $r$ ) ;

process  $PT$  ;

**end** *postorder*.